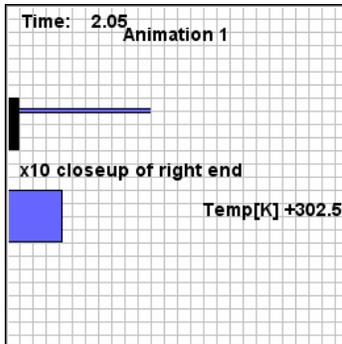


## Worksheet for Exploration 19.2: Expansion of Materials



A rod is fixed at one end. In the animation you see both the rod and a magnified view of the right end (**position is given in meters, time is given in minutes, and temperature is given in kelvin**). As you increase the temperature, notice that the rod increases in length. This Exploration will help you develop a quantitative relationship for the increase in the length of the rod, as a function of the initial length and the temperature change, that holds for all materials. [Restart](#).

Note that the x10 closeup means that a reading (in meters) really is in tenths of meters.

- a. For animation 1, if you double the length, what happens to the change in length?
- i. For example, try 10 m and 20 m.

$$\Delta L_{10} = \underline{\hspace{2cm}}$$

$$\Delta L_{20} = \underline{\hspace{2cm}}$$

- b. Repeat (a) for the material in Animation 2. How do the two results compare?

$$\Delta L_{10} = \underline{\hspace{2cm}}$$

$$\Delta L_{20} = \underline{\hspace{2cm}}$$

- c. How does changing the final temperature change the expansion? (if you double the *change in temperature*, what happens to the change in length?)
- i. Do this for both materials for several final temperatures. Keep the initial length constant.

$T_f$ material 1	$\Delta T_1$	$\Delta L_1$

$T_f$ material 2	$\Delta T_2$	$\Delta L_2$

- d. What general expression can you now write for the change in length as a function of the temperature change and initial length?

The difference between the two materials is described by a different coefficient of linear expansion,  $\alpha$ . For the material in Animation 1  $\alpha$  is  $30 \times 10^{-6}/K$ , while for the material in Animation 2  $\alpha$  is  $20 \times 10^{-6}/K$ .

When heated, a solid (even a thin rod as above), expands in all three dimensions. The equation for the volume expansion is similar to the linear expansion case with the coefficient of expansion approximately equal to  $3\alpha$ .

- e. Why didn't you see the expansion of the rod in the other dimensions?